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A review on Simulate Fracture and Ultra-Low Cycle Fatigue in Steel Structures by ABAQUS

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Abstract

In recent years, many advances have been made in fatigue and failure modeling in steel structures. The methods used to simulate failure and fatigue caused by earthquakes in steel structures are based on experimental and semi-empirical methods or conventional fracture mechanics. Semi-empirical methods cannot be generalized to a wide range of structural details, but conventional fracture mechanics can be reliably used only to simulate brittle fractures such as those observed in the Northridge and Kobe earthquakes, where large-scale yielding is absent. Similar to what is described in this paper, physics-based micromodels seek to simulate the fundamental processes of void growth and coalescence and granular shear responsible for very low-cycle fracture and fatigue in structures. These models are relatively free of assumptions about behavior and can be accurately used to simulate fracture and fatigue in a general sense under different conditions. The growth of voids or cracks can cause sudden crack propagation and deterioration of strength on a global scale of structural components. Therefore, these micromodels, relying on fundamental physics, are equally applicable to situations considered as "brittle" or "unbreakable" at the structural or component level. Examples are given to demonstrate the use of one of these models - the Cyclic Void Growth Model (CVGM) - to simulate failure through continuous finite element analyses. © 2017 Journals-Researchers. All rights reserved. (DOI: https://doi.org/10.52547/JCER.5.2.36)

Keyword: crack; fracture energy; low cyclic; fatigue; steel structure

1. INTRODUCTION

It confirmed the significant probability of failure in steel flexural frame joints and the sensitivity of the response to local effects that are difficult to quantify with structural engineering models and conventional fracture mechanics. The SAC investigation [9] and related studies have mitigated the immediate problem of premature brittle fractures through the development of improved connection details that employ tougher materials, and reduced fracture toughness demands. However, even these post-Northridge connections can

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potentially fracture, although in a ductile manner [20]. Moreover, there are many situations outside the scope of the SAC investigation where the fracture is likely to compromise the seismic safety of the system, such as brace and connection fracture in concentrically braced frames or link-column connection fractures in eccentrically braced frames [16].

Finally, as we move further into the realm of performance-based design, methods, and tools are needed to quantify fracture behavior over a range of seismic demands (hazards), as opposed to simply "qualifying" the structure to perform "adequately" for a single limit state. Given the importance of fracture, this paper addresses the issue in a wider scientific context by examining the accuracy, feasibility and validity of traditional and evolving approaches to characterize earthquake-induced fracture in steel structures. The approaches discussed in this paper encompass various scales of simulation (micro to structure scale), levels of sophistication, and computational resources required to predict fracture. Some important questions are (1) Are traditional fracture and fatigue prediction techniques accurate and general enough to be applied to a wide range of structural configurations under various loading conditions? (2) If not, are more fundamental models available to improve the assessment of fracture? (3) Is application of these advanced computationally feasible? (4) If so, what are the major challenges to the implementation of these models?

This paper briefly and qualitatively describes processes responsible for earthquake-induced fracture, and then reviews the state of the art of earthquake-induced fracture and fatigue prediction in steel structures.

Important limitations of the existing approaches are described and newer physics-based approaches, including the recent development of models for ULCF are introduced. Issues regarding the implementation of these approaches are discussed.

2. EARTHQUAKE-INDUCED FRACTURE DUE TO ULTRA LOW CYCLE FATIGUE AND

REVIEW OF CONVENTIONAL APPROACHES TO PREDICT ULCF

Widespread damage to steel-framed buildings during the 1994 Northridge earthquake confirmed the significant likelihood of fracture in steel moment frame connections and the sensitivity of response to local effects that are difficult to quantify with conventional structural engineering and fracture mechanics models. This section introduces the phenomenon of earthquake-induced ULCF from a physical standpoint and reviews various techniques that are commonly used to characterize ULCF in steel structures, before describing the micromechanics-based approach to ULCF.

Earthquake-induced fracture in structures is typically preceded by a small number of highamplitude cyclic strain or load reversals. Thus, earthquake-induced fracture may be classified as a fatigue problem. The traditional view of fatigue encompasses crack initiation and propagation under a large number of load reversals, ranging from several hundred to a few million cycles. For example, fatigue typically occurs in bridges or mechanical components, where the amplitude of the cyclic demands is small relative to the yield stress of the material and the number of cycles to failure is large. Within this range, fatigue is commonly distinguished between low-cycle and high-cycle fatigue. In contrast to classical high or low-cycle fatigue encountered in bridges or mechanical components, steel structures subjected to earthquakes experience fatigue processes involving fewer than ten cycles with large strain amplitudes, on the order of ten or more times the yield strain. Termed Ultra Low Cycle Fatigue (ULCF), this type of fatigue/fracture occurs in modern steel structures that are designed to absorb seismic energy by sustaining large inelastic deformations under cyclic loads. Plastic hinging of beam-column connections [20] and inelastic cyclic buckling of steel braces [8] are two primary examples where ULCF fracture is the ultimate limit state. An example of ULCF fracture for a steel brace is shown in Fig. 1.

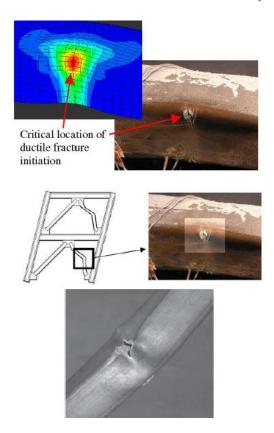


Figure 1. Ultra low cycle fatigue in a concentric steel braces [8]

While ULCF-type behavior has long been recognized in seismic design, the fundamental physical processes responsible for this type of fatigue are not well understood. As a result, earthquake engineering and other situations involving ULCF have relied on various empirical or semi-empirical approaches to evaluate and develop suitable design provisions. While these approaches work well for a given structural detail or loading history, they cannot be generalized conveniently and may be expensive.

3. Experiment-Based Modeling

The most popular approaches to assess the fracture susceptibility of steel structures and components Are Experiment-based empirical methods. These approaches involve testing structural subassemblies under pre-defined monotonic or cyclic loading protocols and then using gross measures of

deformations (inter-story drift, joint rotation) to establish performance limits, and to predict fracture or fatigue capacity.

Experiment-based modeling is attractive mainly because, for a given component, it is relatively free from assumptions except an accurate representation of boundary conditions, and incorporates all aspects of behavior and various physical phenomena like local buckling, material variability, contact, gapping, etc. Also, experiment-based modeling is often the only viable approach, mainly because reliable models may not be available to simulate the physical phenomena contributing to response.

Despite its advantages, test-based modeling cannot be easily generalized to structural details that differ significantly from the tested components in terms of geometry or material types. Due to the high cost of tests, sensitivity, and parametric studies and the use of intermittent loading histories are often not possible. Indeed, some judgment is required to generalize experimental results, which may lead to a conservative description of the adequacy of a given component, rather than an assessment of performance across the full spectrum of behavior. Finally, modeling at the component or structural scale does not provide insights into local effects that may be responsible for the fracture.

4. Conventional Fracture and Fatigue Mechanics

Conventional fracture mechanics (CFM) typically involves the determination of a single parameter at a crack tip that is assumed to quantify the fracture toughness demand.

Consequently, the fracture toughness capacity, too, is expressed in terms of a similar parameter. The toughness demand parameter (such as the stress intensity factor KI, or the -integral, or the Crack Tip Opening Displacement – CTOD), is typically determined either through analytical formulae or finite element simulations. The corresponding material toughness capacity KIC or JIC (critical stress intensity factor or J-integral), is typically determined from standard tests. The fracture toughness typically corresponds to the energy release rate (per unit advance of the crack front). Conventional fracture mechanics is further classified as Linear Elastic

Fracture Mechanics (LEFM – featuring KI) and Elastic-Plastic Fracture Mechanics (EPFM – featuring J and CTOD), suitable for different levels of crack-tip plasticity.

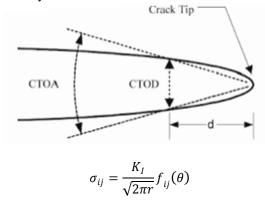


Figure 2. Conventional fracture mechanics methods (a) linear elastic fracture mechanics and (b) crack tip opening displacement – elastic plastic fracture mechanics

While CFM has been used extensively by mechanical and aerospace research and practice, efforts to apply these approaches to civil structures have been fairly recent [4], where CFM-type approaches were used to characterize the fracture susceptibility of pre- and post-Northridge beam-column connection details.

CFM methods are more general as compared to experiment-based methods, mainly because they are based on fairly local stress and strain fields, and, in concept, characterize resistance to fracture at the material level, rather than at the component level.

In fact, the Chi study demonstrated that CFM-type approaches could be used to characterize the ductility of pre-Northridge-type details.

Despite their advantages, CFM approaches have several limitations. For example, they can reliably describe the fracture process only in situations where the yielding is limited in extent, and when a sharp crack is present. They are less suited to conditions of large-scale yielding or details without sharp cracks, such as commonly encountered in post-Northridge connection details. Moreover, as discussed earlier, earthquake-induced fracture is a fracture-fatigue interaction problem, and thus CFM type approaches that do not explicitly include the effects of reversed

cyclic loading cannot be conveniently applied to situations of earthquake-induced fatigue.

In addition to the CFM approaches, traditional fatigue mechanics approaches are often adapted and used in conjunction with experimental analysis or finite element methods. These methods can be classified further into strain/stress-life approaches or damage tolerant approaches. The strain life approaches typically involve dividing the loading history at the component or strain level into equivalent cycles of fixed amplitude and then comparing the accumulated cycles to the "strain-life" determined from other experiments on similar details [6]. Such approaches have been used, for example, Liu and Goel [15], who predicted the fatigue life of bracing elements based on slenderness and width- thickness ratios. However, the Uriz and Mahin [24] study applied this approach to a fiber-based local strain history rather than the entire member. Damage-tolerant fatigue approaches [14] are less common in structural engineering, although they are less applicable as well because they rely on CFM approaches such as the Jintegral or stress-intensity factor.

These conventional fatigue mechanics methods, too are somewhat difficult to adapt to ULCF type situations mainly because (1) Strain life approaches are typically difficult to generalize to various components because ULCF is caused by interactions of stress and strain histories (2) ULCF is often accompanied by large scale yielding, which may invalidate stress intensity based ΔK or ΔJ type approaches (3) Earthquake loading histories are extremely random, with very few cycles, making them difficult to adapt to conventional cycle counting techniques such as Rainflow analysis [21] (4) Damage tolerant ΔK type methods typically require the real or presumed presence of an initially sharp crack or flaw, which might be absent in many structural details.

These models (also referred to as "local fracture mechanics") are applied at the continuum level (in contrast to the component or structure level), through interpretations of stress and strain histories that may be computed through detailed finite element analysis. While other approaches are sometimes used to predict fracture at the continuum level through measures such as critical fracture strains, the micromechanics-based models aim to be more sophisticated, by considering

the interactions of multiple stress and strain components that are responsible for ULCF initiation.

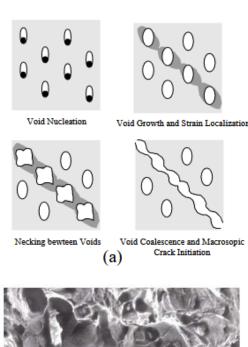
5. The Cyclic Void Growth Model to Predict Earthquake-Induced Ulcf in Steel Structures

summarize the preceding discussion, earthquake-induced fracture in structures presents a complex problem because it involves the complex interactions of material microstructure, irregular loading histories, and uncertainties in crack initiation and subsequent propagation processes. Fundamental micromechanics-based "local" models show promise in predicting fracture and fatigue under such situations, because they are based on the physical processes of void growth and coalescence responsible for ULCF, and therefore are relatively free from many assumptions that limit the applicability of other common approaches. Several such models have been used for ductile fracture conditions under monotonic loading [10, 11, 12, 17, 18]. In addition to focusing on monotonic loading only, all these studies were conducted for pressure vessels and other steels not commonly used in structural engineering. The use of such models in structural engineering has been fairly recent e.g. El-Tawil et al, [7] and Chi et al, [5]. This section discusses the recently introduced Cyclic Void Growth Model (CVGM), and then describes a procedure to apply it along with validation data obtained from a recent NEESR project [13].

For monotonic loading, ductile fracture in steel is caused by the processes of void nucleation, growth, and coalescence [2]. On the application of a triaxial stress field in steel, voids nucleate and grow around inclusions (mostly carbides in the steel material matrix) to coalesce until a macroscopic crack is formed (see Fig. 3). Previous research, Rice and Tracey [19] has shown that void growth is controlled by the equivalent plastic strain, ϵp , and stress triaxiality $T = \sigma m / \sigma e$, where σm is the mean or hydrostatic stress and σe is the von Mises stress.

Equation (1) describes the critical condition of the Void Growth Model (VGM).[20] The numerator in the equation, based on derivations by Rice and Tracey quantifies a void growth that must exceed the void growth capacity critical monotonic VGI to trigger ductile fracture. The void growth demand is based on

stress and strain evolutions at a continuum point and can be determined through detailed FEM analysis, while the void growth capacity can be determined based on tension tests of notched bar specimens [14].



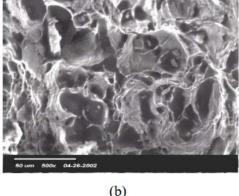


Figure 3. (a) void growth and coalescence leading to ductile fracture in steel and (b) the corresponding dimpled fracture surface [13]

Fracure Index =
$$\frac{\int_{0}^{\varepsilon_{p}} exp(1.5T) d\varepsilon_{p}}{VGI_{monotonic}^{critical}}$$
(1)

While originally proposed for steels used in pressure vessels and nuclear applications, recent studies have validated these models for a large variety of low-carbon structural steels used commonly in civil engineering construction.

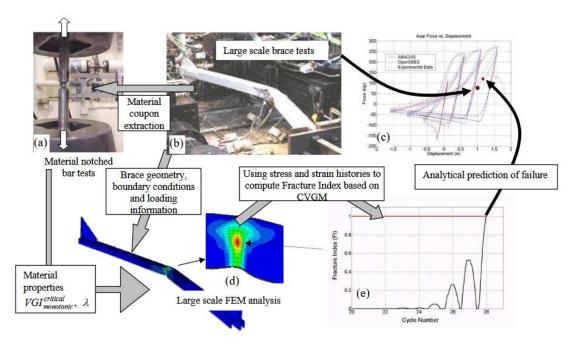


Figure 4. Prediction of ULCF in a concentric brace using the cyclic void growth model [14]

Fracture Index =
$$\frac{\sum_{tensile-cycles} \int_{\varepsilon_{1}}^{\varepsilon_{2}} \exp(|1.5T|) \cdot d\varepsilon_{p} - \sum_{compressive-cycles} \int_{\varepsilon_{1}}^{\varepsilon_{2}} \exp(|1.5T|) d\varepsilon_{p}}{VGI_{monotonic}^{critical} \exp(-\lambda \delta_{p}^{accumulated})} > 1$$
 (2)

For ULCF, both void growth and void collapse need to be explicitly considered, due to the reversed cyclic nature of the load. Recent research led to the development of a model that simulates the micromechanisms of void growth, collapse, and cyclic degradation that are responsible for Ultra Low Cycle Fatigue. Equation (2) describes the critical condition of the CVGM that must be attained to trigger ULCF initiation.

Similar Void Nucleation Void Growth and Strain Localization Necking bewteen Voids Void Coalescence and Macrosopic Crack Initiation (a) (b) to (1), the numerator of the equation reflects the cyclic micromechanical void growth demand and is based on strains and stresses inferred through finite element analysis, and the denominator reflects material capacity, calibrated through convenient small scale tests, such that ULCF is assumed to initiate when the Fracture Index (FI) exceeds 1. The model contains one additional parameter λ (quantifying the rate of

capacity degradation) that is calibrated through multiple cyclic tests of notched bar specimens.

The CVGM model too, has been validated using fractographic studies as well as small, medium and large scale tests, most recently as part of a NEESR project. Because the CVGM and similar models simulate the fundamental physics of the ULCF process, and are applied at a continuum level, rather than the component or structural level, they can be applied in a general sense to a wide variety of structural details to improve their performance.

6. Procedure for predicting Ultra Low Cycle Fatigue in structural components using the Cyclic Void Growth Model

Figure 4 schematically illustrates the various steps/components of predicting ULCF based on CVGM, and their inter-relationships. As discussed

earlier, the Cyclic Void Growth Model has two material parameters (VGI and λ) that can be calibrated from small-scale tests and complementary finite element analysis of notched bar specimens such as the one shown in Fig. 4a. A detailed calibration procedure is discussed in detail in Kanvinde and Deierlein [14]. For a given steel type typically ten experiments (four monotonic and six cyclic) are required to calibrate the two parameters. These experiments usually include different notch sizes to query the effect of stress state or triaxiality (sharper notches result in higher triaxiality).

Once the parameters have been calibrated, detailed finite element analysis of large scale components can be conducted to determine the stress and strain histories at each continuum point within the component. Recently, the authors tested 19 large-scale concentric brace elements cyclically to validate the CVGM model for full scale specimens. Hollow bracing elements typically undergo inelastic cyclic buckling followed by local buckling of the cross section leading to large strain amplification, and eventually ULCF induced fracture [8].

Thus, they present an ideal test-bed to validate the CVGM model. Figure 4b shows a photograph of a representative brace specimen as it buckles, while Fig. 4c includes the axial load deformation plot for the specimen, as well as the instant during the loading history when fracture initiation was first observed (marked by a star symbol). Figure 4d shows a FEM simulation (performed on ABAQUS [1]) of this specimen (the brace is a 10-foot-long HSS 4X4X1/4 shape). The simulation considers all the relevant aspects of behavior, and features multiaxial plasticity with combined isotropic and kinematic hardening. The parameters for the plasticity model are inferred from the small scale coupon tests. To simulate the local buckling accurately, initial imperfections must be prescribed to perturb the analysis. Initial imperfections are inputted into the model by scaling the appropriate global and local buckling modes of the brace to measure the imperfections of the experimental specimen. A simulation-based load deformation plot is overlaid on the experimental plot in Fig. 4c, and the agreement between the two is very good.

To predict the location and instant of ULCF initiation, the stress and strain histories are determined from the FEM simulation over the entire plastic hinge

region as the loading progresses, and the Fracture Index (FI) is determined as per (2) at each loading step. It is important to note that FI is determined at each continuum location in the FEM model and is dependent on material parameters (VGI critical monotonic and λ). Thus, the FI can be determined in a general sense for any component once the material properties have been calibrated using the small scale tests. ULCF is assumed to initiate at a given continuum location when the micromechanical cyclic void growth demand exceeds degraded void size capacity, or mathematically, FI at that location exceeds 1. Fig. 4e plots the FI at the critical location in the locally buckled cross-section profile (indicated by the arrow in Fig.4d), versus the loading time step. The instant when FI exceeds 1 for the first time is recorded as the analytical prediction of ULCF initiation. This point is shown as circle on Fig. 4c. Comparing this point to the experimental fracture instant (shown as a circle in the figure) demonstrates the accuracy of the ULCF models. Furthermore, as is evident from Fig. 4c, the instant of ductile crack initiation predicted from the analysis is very close to that observed during the experiment. Moreover, the physical location of ULCF is predicted with exact precision by the CVGM model.

As noted in Fig. 4c, the CVGM model successfully predicts the point of ULCF initiation in the experiment. Α similar agreement experimental and analytical fracture is observed for all 19 specimens. Given that the test matrix included specimens with different cross-section geometries, different steel materials, and loading histories, the good agreement between experimental and CVGM predictions of the fracture indicates that the CVGM does indeed capture fundamental physical processes and material properties that control fracture. Thus, once material properties are determined using smallscale tests, the CVGM can be applied in a general sense across a range of component geometries, materials and loading histories.

7. AREAS FOR REFINEMENT OF THE MICROMECHANICS BASED MODELING APPROACH

While the CVGM and similar micromechanical models provide a fairly general and accurate

framework for predicting earthquake induced fracture in steel structures, there are several issues that need to be addressed to successfully and routinely apply these models in structural simulations. Some of these issues concern the level of sophistication of the FEM simulation, while others are related to the accuracy of the micromechanics- based model itself. Some of these issues are now summarized.

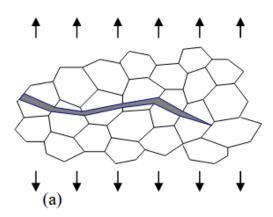
Because the micromechanics-based models are applied at the continuum level, their success is contingent on an accurate characterization of the local stress and strain histories at critical locations. Thus, sophisticated modeling of various phenomena that affect these stresses and strains is required. For example, the brace specimens described in this paper required simulation of global and local buckling, which in turn required a detailed definition of initial member imperfections. One can envision that in other situations, various mechanisms may become critical, e.g. gapping and contact in connections including fillet welds, or the loosening of bolts in bolted connections. In addition to this, multiaxial cyclic plasticity model typically need to be calibrated and used for accurate material constitutive response.

In many situations such as welded connections (that include base and weld metal and heat affected zones) it is necessary to consider the spatial gradients and statistical variability in material properties and capacities that may affect the instant and location of ULCF initiation. The second phase of the NEESR project, uses welded column base plate details as a test-bed and investigates some of these issues.

While the model discussed in this paper addresses mainly ULCF initiation, often the fracture propagates in a ductile manner for a considerable duration of time before the component fractures completely [3]. Thus, methods are required to integrate the initiation models with analytical crack propagation capabilities to achieve more realistic estimates of performance.

Another important issue to consider with regard to the micromechanics-based models is that they typically focus on a single mechanism for failure (e.g. microvoid growth and coalescence). However, depending on stress conditions and material properties, various other mechanisms may be possible, such as intragranular cleavage (Fig. 5a) or intergranular fracture (Fig 5b). In fact, in many cases fracture may initiate as ductile microvoid growth type

fracture, and transition to brittle cleavage as the crack grows [3]. Thus, appropriate models need to be chosen for a given situation. For most ductile structural components, without sharp cracks or flaws, fracture typically initiates due to microvoid growth, and the CVGM may be appropriate for such situations.



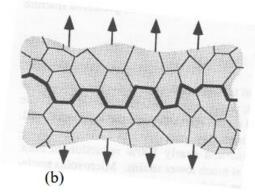


Figure 5. Other mechanisms of fracture – (a) Intragranular cleavage and (b) Intergranular fracture– adapted from Anderson 1995 [2]

Thus, while the micromechanics-based models offer an attractive and physics-based approach to predicting ULCF, they also require more sophisticated modeling of many physical phenomena and knowledge of potential micromechanisms of failure. Moreover, for sharp crack type situations, where the stress gradients are high, these methods typically require characterizing stresses and strains with a high spatial resolution, often requiring significant computational resources. However, given the cost of experimentation, and the decreasing cost of

computational technology, these approaches will likely become more widespread in the future.

8. SUMMARY

This paper reviews various methods to predict earthquake-induced fracture in steel structures, and presents the physics-based micromechanical approach as a general, accurate and viable approach. Earthquake-induced fracture in structures is an important limit state, often controlling the ductility of the structural system. Unlike high-cycle fatigue or low-cycle fatigue observed in bridges or mechanical components that are subjected to thousands or millions of cycles, earthquake-induced Ultra-Low Cycle Fatigue (ULCF) is characterized by a very small number (<10) of random, high amplitude cycles. However, fundamental approaches to predict ULCF in steel structures are not well developed.

Traditional models to characterize earthquakeinduced fracture have relied on experimental or empirical approaches, or on adaptation of techniques originally developed for other problems (such as highcycle fatigue). Consequently, predictions from these models cannot be generalized to components and situations beyond those that are experimentally tested. Moreover, these costly approaches do not provide insights into local effects that are responsible for fracture. More recently, Conventional Fracture Mechanics (CFM) methods have been used to assess the fracture susceptibility of structural components. While an improvement over experiment-based methods, the CFM methods are limited by assumptions of small-scale yielding and monotonic loading that are not typical to ductile details subjected to earthquake-type ULCF.

Physics-based models that simulate the fundamental micromechanics of the fracture- ULCF process are presented as an attractive alternative to traditional methods. These are fracture criteria based on continuum stress and strain quantities, and thus can be applied to a variety of structural details once the material properties are calibrated. The Cyclic Void Growth Model (CVGM), presented in this paper is one such model that simulates the micromechanical processes of cyclic void growth, collapse and damage

to predict ULCF initiation. The application of the CVGM model requires the calibration of two material parameters. This is done through fairly economical small scale notched bar cyclic tests. A procedure for predicting ULCF initiation based on CVGM is outlined, and validation experiment results are presented which suggest that the CVGM simulates fundamental material behavior and can be applied in a general sense to a wide variety of structural components and configurations.

However, being highly dependent on the accurate characterization of local stress and strain histories, these micromechanical models require the simulation of other physical processes such as global and local buckling, contact, gapping etc. Also important are aspects such as the spatial gradients and statistical variability in material properties.

Moreover, these models are typically focused on a single micromechanism, so multiple models (e.g. addressing void growth, cleavage) may need to operate simultaneously for an accurate simulation.

It is important to note that micromechanics-based earthquake-induced fracture prediction approaches are relatively recent, and need refinement to be widely accepted.

However, given their fundamental appeal, flexibility and generality, coupled with the research community's shift towards model-based simulation, they may be a viable alternative to experimental approaches in the future.

Acknowledgments

A true friend accepts who you are, but also helps you become who you should be. I do appreciate my wife who is my real true friend.

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